

Date Planned : __ / __ / __	Daily Tutorial Sheet - 10	Expected Duration : 90 Min
Actual Date of Attempt : __ / __ / __	Level - 2	Exact Duration : _____

- \*186. The number of ways in which 5 different prizes can be distributed amongst 4 persons if each is entitled to receive at most 4 prizes is:
- (A) 1020                      (B) 620                      (C)  $5^4 - 5$                       (D)  $4^5 - 4$
- \*187. A letter lock consists of 3 rings marked with 15 different letters. If N denotes the number of ways in which it is possible to make unsuccessful attempts to open the lock, then:
- (A) 482 divides N                      (B) N is product of 3 distinct prime numbers  
 (C) N is product of 4 distinct prime numbers                      (D) N is product of 2 distinct prime numbers
- \*188. The number of zeroes at end of  $70!$  is equal to:
- (A) The number of 6-digit numbers formed using all the digits 1, 2, 3, 4, 5, 6 divided by  $^{10}C_2$   
 (B) The number of 6-digit numbers formed using all the digits 1, 2, 3, 4, 5, 6 divided by 10.  
 (C) Twice the number of 4-digit numbers formed using 4 of the digits 1, 2, 3, 4, 5, 6 divided by  $^{10}C_2$   
 (D) The number of 4-digit numbers formed using 4 of the digits 1, 2, 3, 4, 5, 6 divided by 5
189. There are three papers of 100 marks each in an examination. Then the no. of ways can a student get 150 marks such that he gets atleast 60% in two papers:
- (A)  ${}^3C_2 \times {}^{32}C_2$                       (B)  ${}^4C_3 \times {}^{32}C_2$                       (C)  ${}^4C_3 \times {}^{36}C_2$                       (D)  ${}^4C_3 \times {}^{36}C_3$
- \*190. X is a set containing n elements. A subset  $P_1$  is chosen at random and then set X is reconstructed by replacing the elements of set  $P_1$ . A subset  $P_2$  of X is now chosen at random and again set X is reconstructed by replacing the elements of  $P_2$ . This process is continued to choose subsets  $P_3, P_4, P_5, \dots, P_m$  where  $m \geq 2$ , then the number of ways to select sets such that:
- (i)  $P_i \cap P_j = \phi$  for  $i \neq j$  and  $i, j = 1, 2 \dots m$ .                      (ii)  $P_1 \cap P_2 \cap P_3 \dots \cap P_m = \phi$
- \*191. 10 different toys are to be distributed among 10 children. Total number of ways of distributing these toys so that exactly 2 children do not get any toy, is equal to:
- (A)  $(10!)^2 \left( \frac{1}{3! 2! 7!} + \frac{1}{(2!)^5 6!} \right)$                       (B)  $(10!)^2 \left( \frac{1}{3! 2! 7!} + \frac{1}{(2!)^4 6!} \right)$                       (C)  $(10!)^2 \left( \frac{1}{3! 7!} + \frac{1}{(2!)^5 6!} \right)$                       (D)  $(10!)^2 \left( \frac{1}{3! 7!} + \frac{1}{(2!)^4 6!} \right)$
192. Identify following statements for True (T) and False (F):
- S<sub>1</sub>:** An old man while dialing a 7-digit telephone number remembers that the first four digits consist of one 1's, one 2's and two 3's. He also remembers that the fifth digit is either a 4 or 5 while has no memory of the sixth digit, he remembers that the seventh digit is 9 minus the sixth digit. Maximum number of distinct trials he has to try to make sure that he dials the correct telephone number, is 240.
- S<sub>2</sub>:** A woman has 11 close friends. The number of ways in which she can invite 5 of them to dinner, if two of them are not on speaking terms and will not attend together is 378.
- S<sub>3</sub>:** 10 IIT and 2 PET students sit in a row. If the total number of ways in which exactly 3 IIT students sit between 2 PET students is  $\lambda \times 10!$ , then  $\lambda$  is 6.
- Which of the following choice is correct?
- (A) TTT                      (B) TTF                      (C) TFF                      (D) FTF

- 193.** There are 10 stations on a circular path. A train has to stop at 4 stations such that no two stations are adjacent. The number of such selections must be: ▶
- (A) 25                      (B) 35                      (C) 210                      (D) 50
- 194.** Number of ways of arranging 12 boys and 12 girls are as follows: ▶
- $a_1$  = a line such that boys and girls sit alternatively.  
 $a_2$  = around a circular table alternatively.  
 $a_3$  = around an equilateral triangular table alternatively and eight on each side.  
 $a_4$  = around a square table alternatively and six on each side.
- (For  $a_3$  and  $a_4$  on a corner if on one side, it's a boy then on the other side it should be a girl to maintain alternation). Which of the following is true?
- (A)  $a_1 > a_2 > a_3 > a_4$                       (B)  $a_4 > a_3 > a_2 > a_1$   
 (C)  $a_1 > a_3 > a_4 > a_2$                       (D)  $a_1 > a_4 > a_3 > a_2$
- 195.** The number of different ways the letters of the word VECTOR can be placed in 8 boxes given below such that no row empty is equal to:
- |  |  |  |  |
|--|--|--|--|
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
- (A) 26                      (B)  $26 \times 6!$                       (C)  $6!$                       (D)  $2! \times 6!$
- \*196.** A man has to move 9 steps. He can move in 4 directions: left, right, forward, backward. In how many ways he can move 9 steps such that he finishes his journey one step away (either left or right or forward or backward) from the starting position? ▶
- (A)  $\left({}^{10}C_5\right)^2$                       (B)  $4 \times \left({}^9C_4\right)^2$                       (C)  $\left({}^9C_4\right)^2$                       (D)  $4 \times \left({}^{10}C_5\right)^2$
- 197.** How many integral solutions are there to the system of equations  $x_1 + x_2 + x_3 + x_4 + x_5 = 20$  and  $x_1 + x_2 + x_3 = 5$  when  $x_k \geq 0$ ? ▶
- (A) 334                      (B) 336                      (C) 332                      (D) 338
- 198.** Three girls and nine boys need to be seated in two vans, each having numbered seats, 3 in the front and 4 at the back. How many seating arrangements are possible if 3 girls should sit together in a back row on adjacent seats? ▶
- (A)  $12!$                       (B)  $2 \times 12!$                       (C)  $2 \times 10!$                       (D)  $2 \times 9!$
- 199.** If  $n_1$  and  $n_2$  are five- digit numbers, the total number of ways of forming  $n_1$  and  $n_2$  so that these numbers can be added without carrying at any stage is: ▶
- (A)  $45(55)^4$                       (B)  $38(55)^4$                       (C)  $36(55)^4$                       (D)  $40(55)^4$
- 200.** Number of sub parts into which 'n' straight lines in a plane can divide it is: ▶
- (A)  $\frac{n^2 + n + 2}{2}$                       (B)  $\frac{n^2 + n + 4}{2}$                       (C)  $\frac{n^2 + n + 6}{2}$                       (D) None of these